

190

SOME CONCEPTS ON THE USE OF
DEFLECTION MEASUREMENTS FOR
EVALUATING FLEXIBLE PAVEMENTS

SEPT. 1961

NO. 26

Joint
Highway
Research
Project

by
R. D. WALKER

E. J. YODER

PURDUE UNIVERSITY
LAFAYETTE INDIANA



Digitized by the Internet Archive
in 2011 with funding from
LYRasis members and Sloan Foundation; Indiana Department of Transportation



LIST OF FIGURES

Figure

Caption

1. Deflection Profiles Under Dual Wheels
2. Deflection (mm) - Measured and Calculated
3. Comparison of Measured and Calculated Deflection
4. Measured Deflection Profiles
5. Calculated Deflection Profiles
6. Comparison of Measured and Calculated Deflection
7. Measured Deflection Profiles
8. Calculated Deflection Profiles
9. Comparison of Measured and Calculated Deflection



to the fact that the system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.

The system is not yet fully developed.



Problem 1: Solving a System of Linear Equations

Consider the following system of linear equations:

$$\begin{cases} x + 2y + 3z = 10 \\ 2x + 3y + 4z = 15 \\ 3x + 4y + 5z = 20 \end{cases}$$

Find the values of x , y , and z that satisfy all three equations.

Hint: You can solve this system using Gaussian elimination or matrix methods.

Write down your solution for x , y , and z .

Check your solution by substituting the values back into the original equations.

What is the value of x ?

What is the value of y ?

What is the value of z ?

What is the value of $x + y + z$?

What is the value of $2x + 3y + 4z$?

What is the value of $3x + 4y + 5z$?

What is the value of $x^2 + y^2 + z^2$?

What is the value of $x^3 + y^3 + z^3$?

What is the value of $x^4 + y^4 + z^4$?

What is the value of $x^5 + y^5 + z^5$?

What is the value of $x^6 + y^6 + z^6$?

What is the value of $x^7 + y^7 + z^7$?

What is the value of $x^8 + y^8 + z^8$?

What is the value of $x^9 + y^9 + z^9$?

What is the value of $x^{10} + y^{10} + z^{10}$?

What is the value of $x^{11} + y^{11} + z^{11}$?

What is the value of $x^{12} + y^{12} + z^{12}$?

What is the value of $x^{13} + y^{13} + z^{13}$?



REPORT OF INVESTIGATION

The purpose of this investigation was to determine the effect of the proposed change in the method of determining the amount of the deduction for the interest on the mortgage on the amount of the deduction for the interest on the mortgage. The investigation was conducted by the Internal Revenue Service, Department of the Treasury, and the results are set forth in this report.

SUMMARY OF FACTS

The following facts were ascertained from the records of the Internal Revenue Service, Department of the Treasury, and the results are set forth in this report.

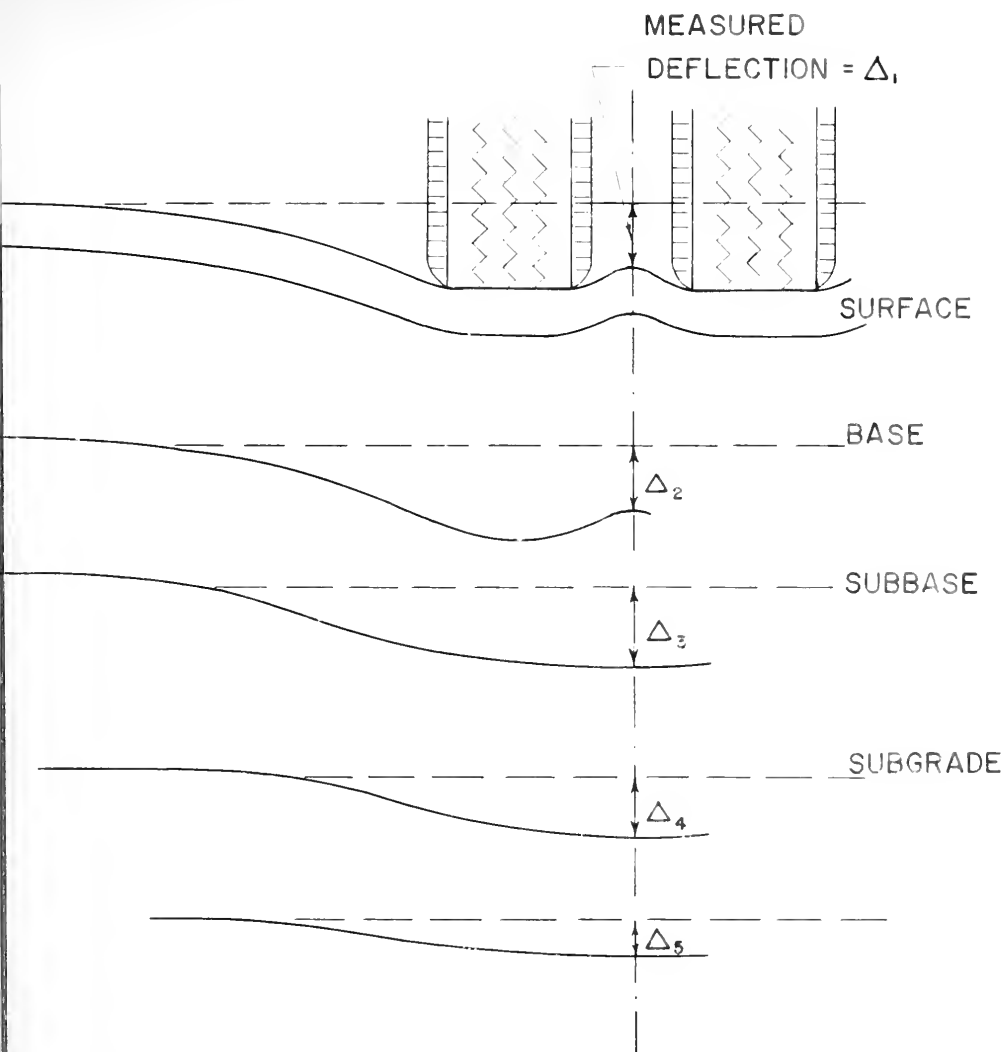
The amount of the deduction for the interest on the mortgage is determined by the amount of the mortgage interest paid during the year. The amount of the mortgage interest paid during the year is determined by the amount of the mortgage interest paid during the year.

The amount of the deduction for the interest on the mortgage is determined by the amount of the mortgage interest paid during the year. The amount of the mortgage interest paid during the year is determined by the amount of the mortgage interest paid during the year.

The amount of the deduction for the interest on the mortgage is determined by the amount of the mortgage interest paid during the year. The amount of the mortgage interest paid during the year is determined by the amount of the mortgage interest paid during the year.

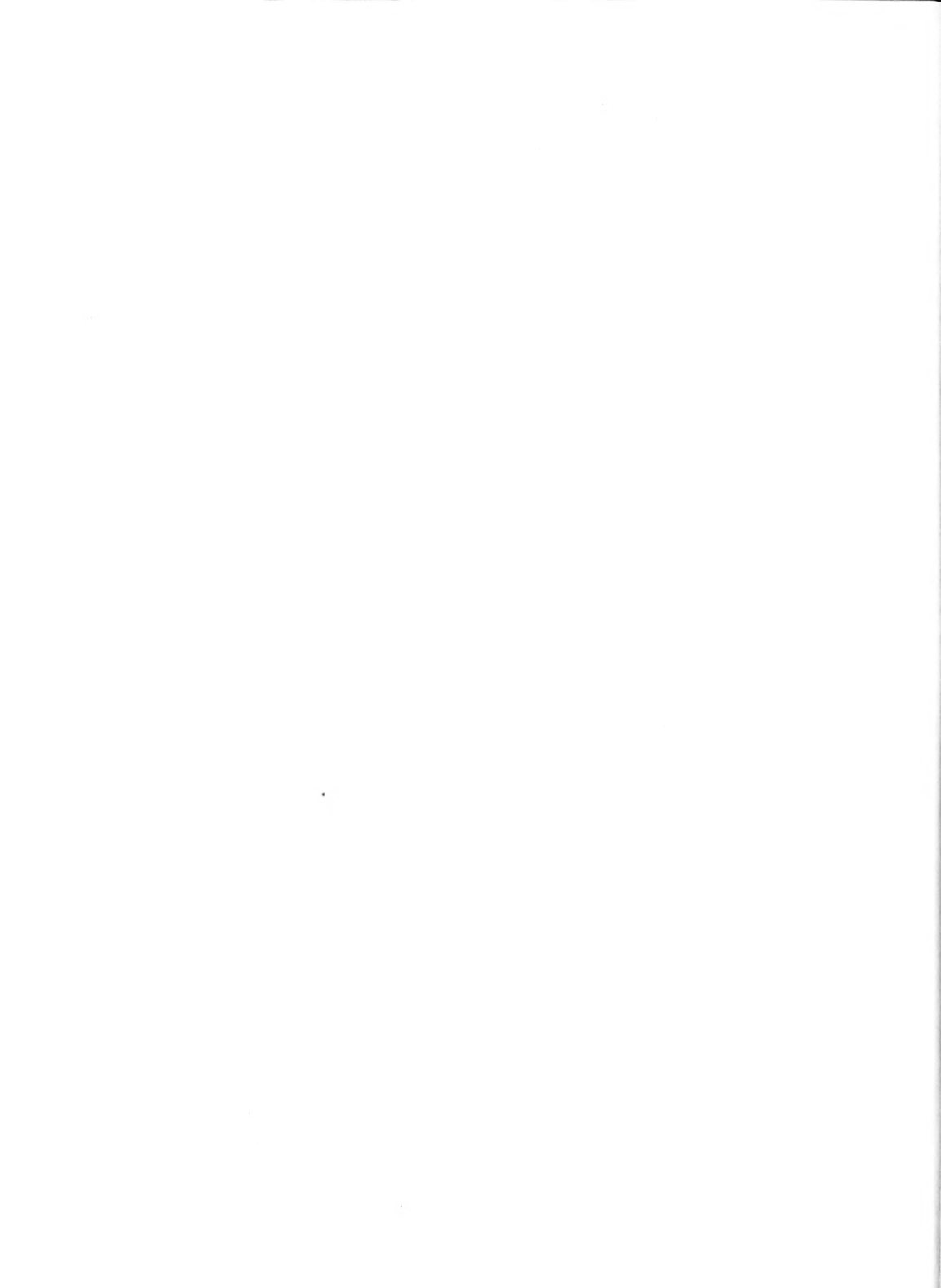
The amount of the deduction for the interest on the mortgage is determined by the amount of the mortgage interest paid during the year. The amount of the mortgage interest paid during the year is determined by the amount of the mortgage interest paid during the year.

The amount of the deduction for the interest on the mortgage is determined by the amount of the mortgage interest paid during the year. The amount of the mortgage interest paid during the year is determined by the amount of the mortgage interest paid during the year.



DEFLECTION PROFILES

FIGURE 1



Parasitic distress is evidenced by rubbing, crawling, etc. - can be caused by insects, fungi, bacteria, etc. distress can be caused by other factors, e.g. rubbing, etc. - consider the rubbing caused in Figure 1. It is noted that showing between the wheels could cause the formation of a sharp ridge, or an effect that can be considered as "rubbing" - could be a factor, even though it is not a direct cause of the distress.

It is noted that the rubbing between the wheels could cause the formation of a sharp ridge, or an effect that can be considered as "rubbing" - could be a factor, even though it is not a direct cause of the distress. The rubbing between the wheels could cause the formation of a sharp ridge, or an effect that can be considered as "rubbing" - could be a factor, even though it is not a direct cause of the distress. The rubbing between the wheels could cause the formation of a sharp ridge, or an effect that can be considered as "rubbing" - could be a factor, even though it is not a direct cause of the distress.

It is noted that the rubbing between the wheels could cause the formation of a sharp ridge, or an effect that can be considered as "rubbing" - could be a factor, even though it is not a direct cause of the distress.

It is noted that the rubbing between the wheels could cause the formation of a sharp ridge, or an effect that can be considered as "rubbing" - could be a factor, even though it is not a direct cause of the distress. The rubbing between the wheels could cause the formation of a sharp ridge, or an effect that can be considered as "rubbing" - could be a factor, even though it is not a direct cause of the distress. The rubbing between the wheels could cause the formation of a sharp ridge, or an effect that can be considered as "rubbing" - could be a factor, even though it is not a direct cause of the distress.



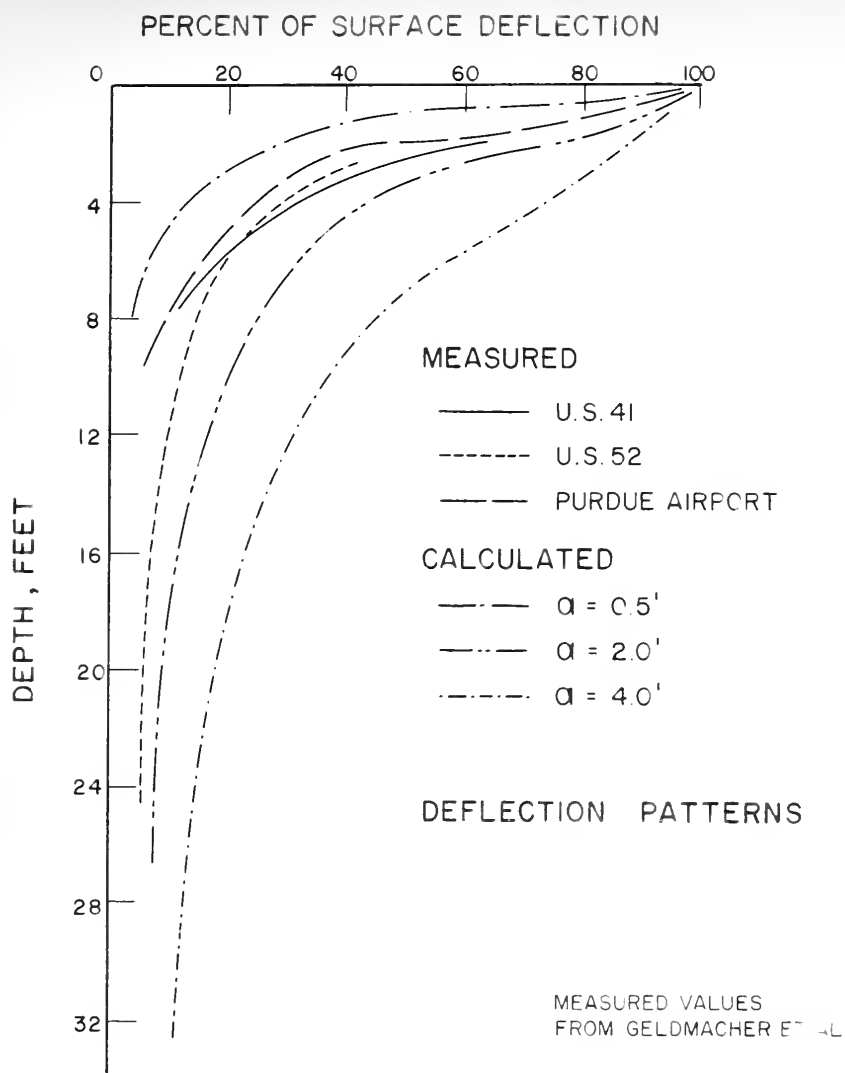


FIGURE 2



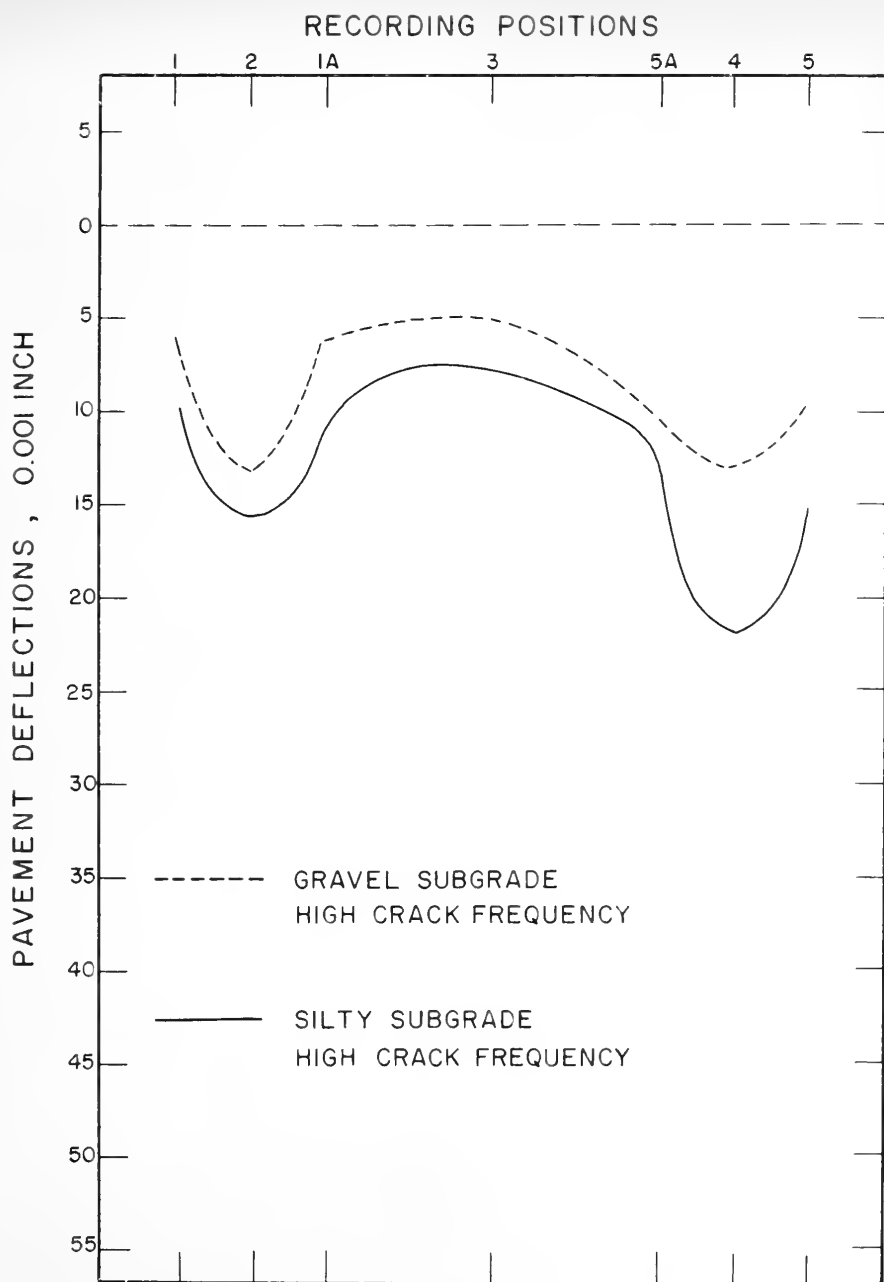
total load (which fix the radius), vertical deflection is dependent upon a settlement factor F which is in turn dependent upon the ratio of z/a . The above equation was developed using certain boundary conditions which will not be discussed here. Considering the theoretical or calculated values in Figure 2, depth of influence of deflection for various plate sizes is shown. For example, circular plates with large diameters would require depths of soil well below the surface of soil to be considered. The curves given are for $\nu = 0.2$, and $E = 10^{10}$.

Figure 3 shows the effect of the ratio of z/a on the settlement factor F . The curves are for $\nu = 0.2$ and $E = 10^{10}$. The curves show that the settlement factor F increases with the ratio of z/a . The curves also show that the settlement factor F is independent of the ratio of z/a for $z/a > 1.0$. The curves are for $\nu = 0.2$ and $E = 10^{10}$. The curves show that the settlement factor F increases with the ratio of z/a . The curves also show that the settlement factor F is independent of the ratio of z/a for $z/a > 1.0$. The curves are for $\nu = 0.2$ and $E = 10^{10}$.

APPENDIX B - CALCULATION OF DEFLECTION

The purpose of this appendix is to show that the deflection of a beam is used in the calculation of the settlement factor F . The deflection of a beam is used in the calculation of the settlement factor F . The deflection of a beam is used in the calculation of the settlement factor F . The deflection of a beam is used in the calculation of the settlement factor F . The deflection of a beam is used in the calculation of the settlement factor F .

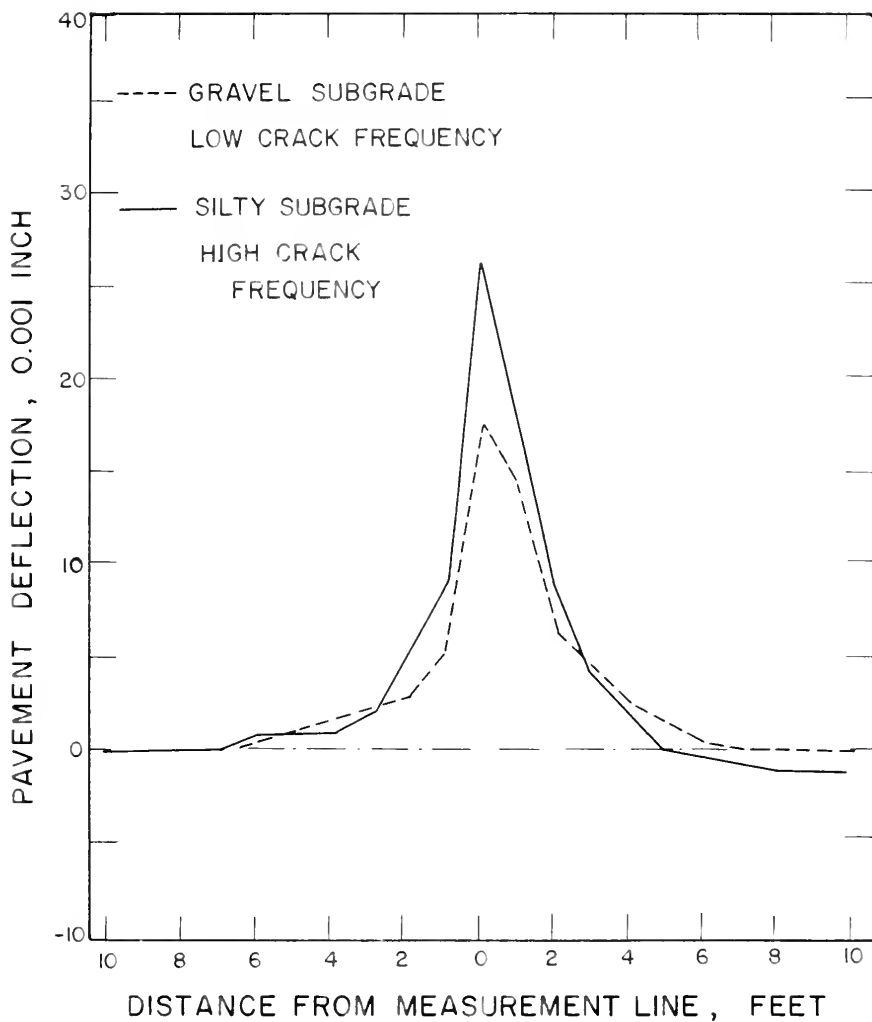




TYPICAL TRANSVERSE DEFLECTION CURVES

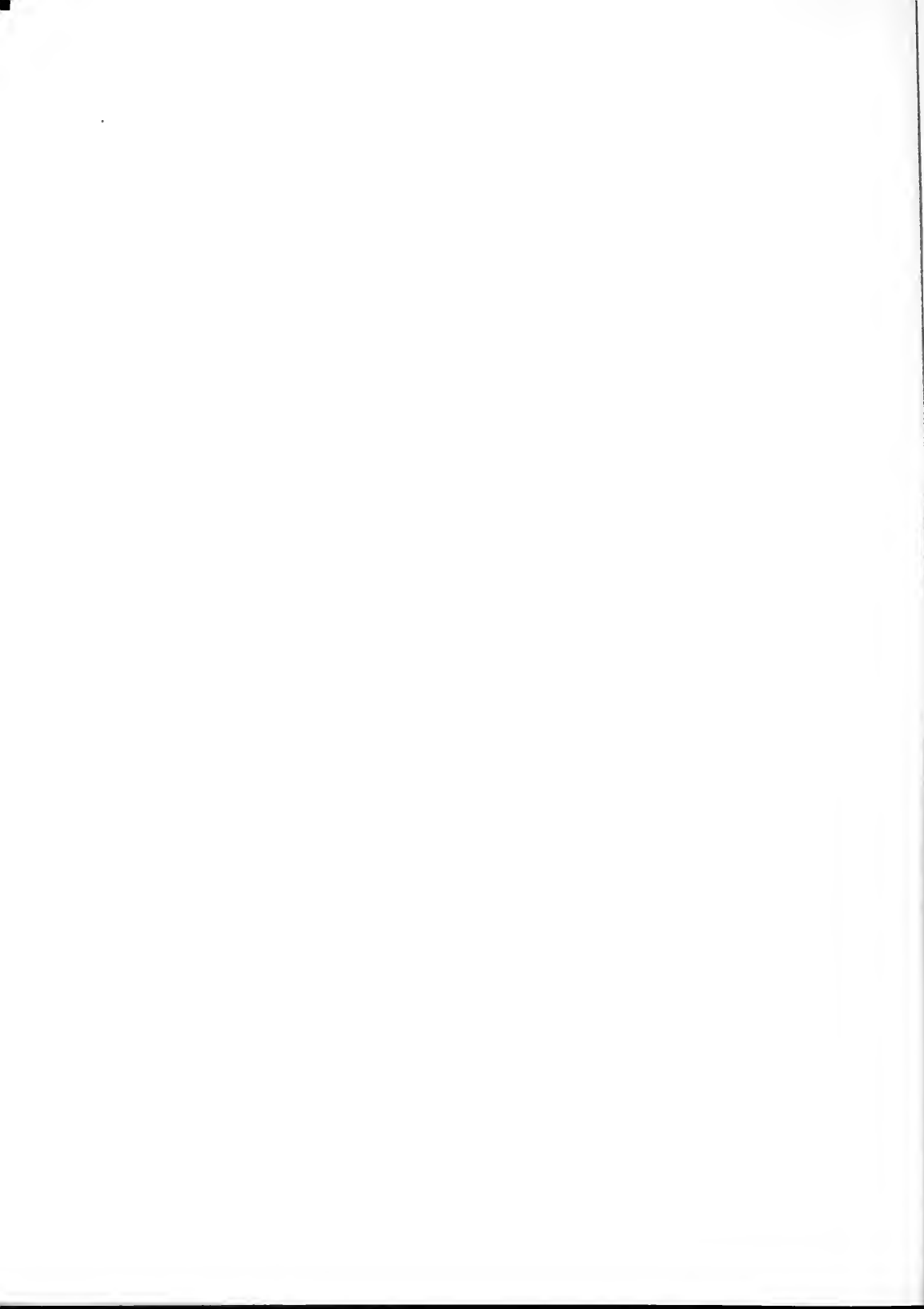
FIGURE 3





TYPICAL LONGITUDINAL
DEFLECTION CURVES

FIGURE 4



No significant correlation was found between total deflection and wheel frequency.

Figure 3 and 4 illustrate an interesting feature of the deflection patterns. In each case the granular subgrade showed less total deflection than the siltier subgrade. However, the radius of bending of the pavement built on the granular subgrade was generally smaller than the radius of bending for the siltier subgrade. This is the opposite of what would be expected if the granular subgrade were stiffer than the siltier subgrade. It is suggested that these results may be due to the fact that the granular subgrade is more uniform in composition than the siltier subgrade, which is more heterogeneous. This is supported by the fact that the radius of bending and pavement distance

Use of wheel deflection (deflection of the lower side of the thickness of the layer) is subject to the restriction that deflection is dependent upon depth below the surface as well as type of material. Thus it becomes necessary to determine a system of correction for varying wheel deflections if they do not fall within the range of correction for a given layer of the pavement.

The use of wheel deflection as a measure of pavement strength is subject to the restriction that it is not a direct measure of strength. It is a measure of the resistance of the pavement to deflection. It is suggested that the use of wheel deflection as a measure of pavement strength is subject to the restriction that it is not a direct measure of strength. It is a measure of the resistance of the pavement to deflection.

Figure 5 illustrates the effect of wheel deflection on the radius of bending. The equation shown in the figure is a curve which is a function of wheel deflection. It is suggested that the use of wheel deflection as a measure of pavement strength is subject to the restriction that it is not a direct measure of strength. It is a measure of the resistance of the pavement to deflection.



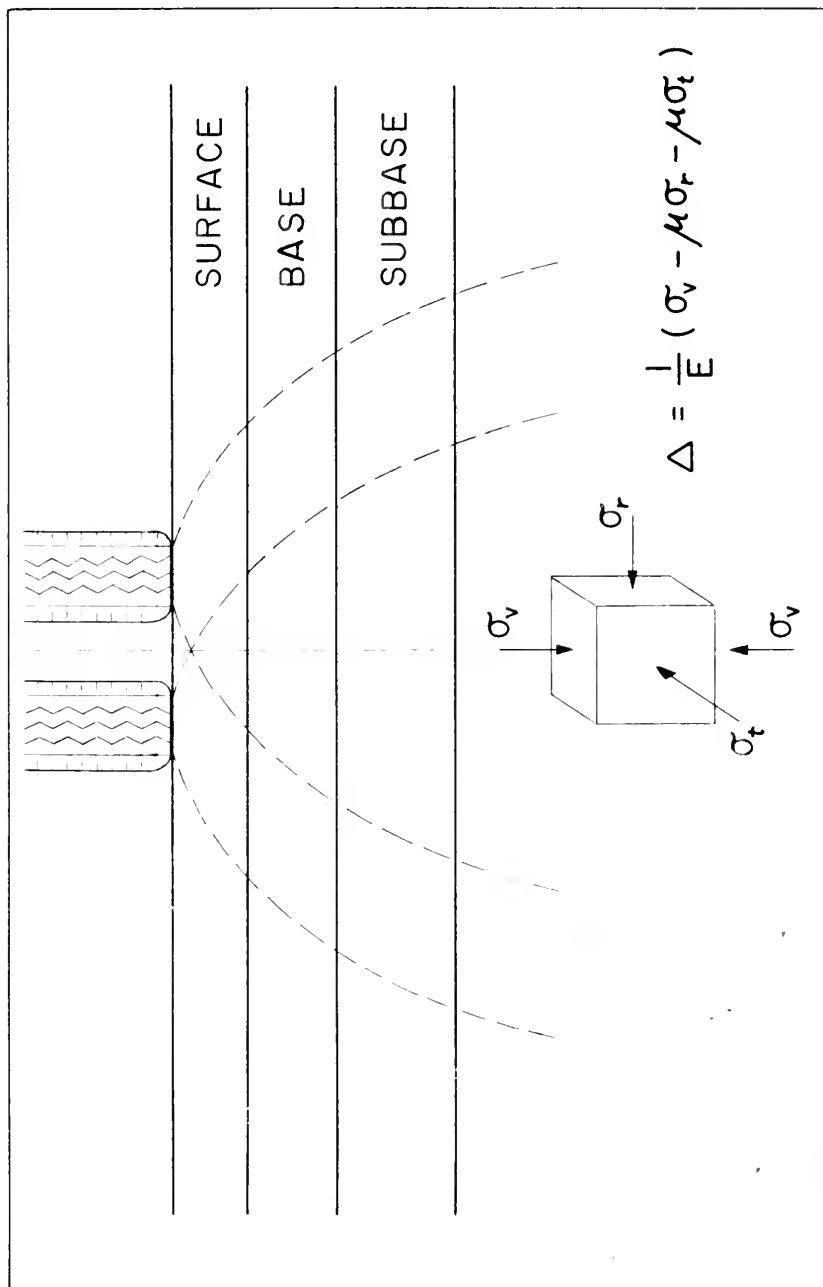


FIGURE 5



stresses in the soil. It is necessary to have a single value to allow for modulus of elasticity. Unfortunately, this requires a great deal of the engineer's knowledge.

Figure 6 shows variation of vertical stress with depth as measured by pressure cells below a 12-inch crushed stone base course. "Inconsistencies" values of stress are also plotted against depth. It is noted that the values are not too far from the theoretical stress values. However, in the case of the stress pattern in the subgrade, it is necessary to use the change of stress with depth to compute an elastic modulus. It appears that use of theoretical equations for estimating stresses is warranted.

STRESS MEASUREMENTS

Using the procedure, a series of stress measurements were made on a certain type of soil. The results are shown in Figure 7. It is noted that the values are not too far from the theoretical stress values. However, in the case of the stress pattern in the subgrade, it is necessary to use the change of stress with depth to compute an elastic modulus. It appears that use of theoretical equations for estimating stresses is warranted.

A research project was conducted whereby the vertical stress was measured on the U. S. 31 Test Facility using the Field Cell. Figure 8 shows a diagrammatic sketch of this test. The probe at the extreme left-hand side is placed between a set of steel wheels and then as the wheel moves away from the probe, deflection as indicated by means of the dial on the right.

Figure 8 shows the set-up for measuring the layer deflections. The test pavement consists of asphaltic concrete, water-bound macadam and granular subbase resting upon the grade. Holes were drilled through the asphaltic concrete and plates were set on each pavement layer.



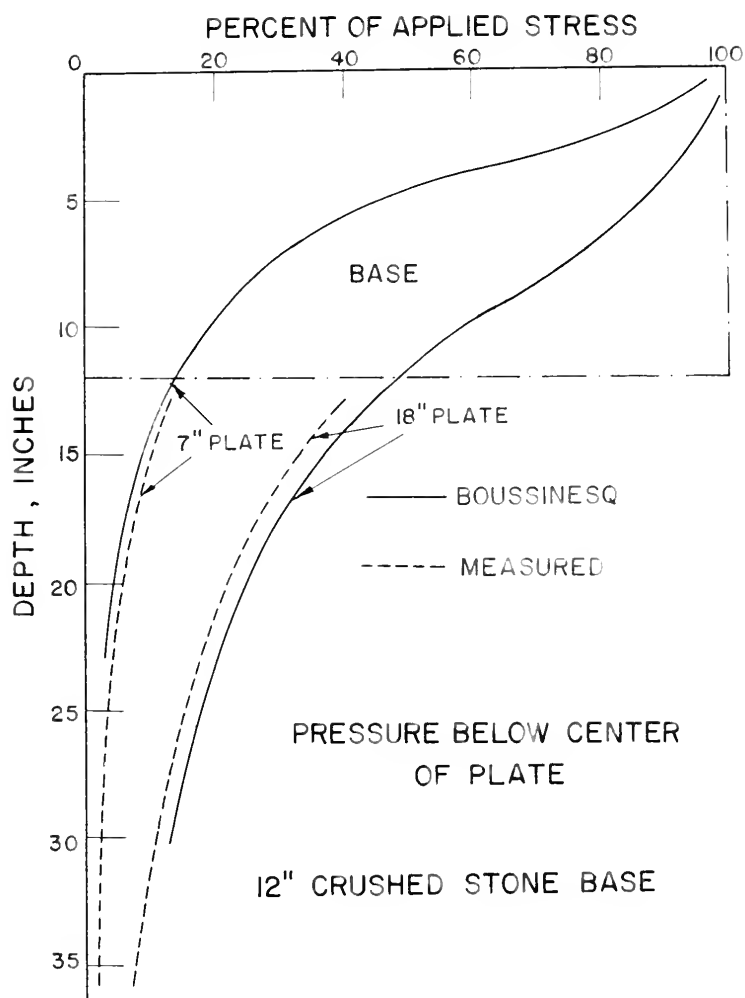
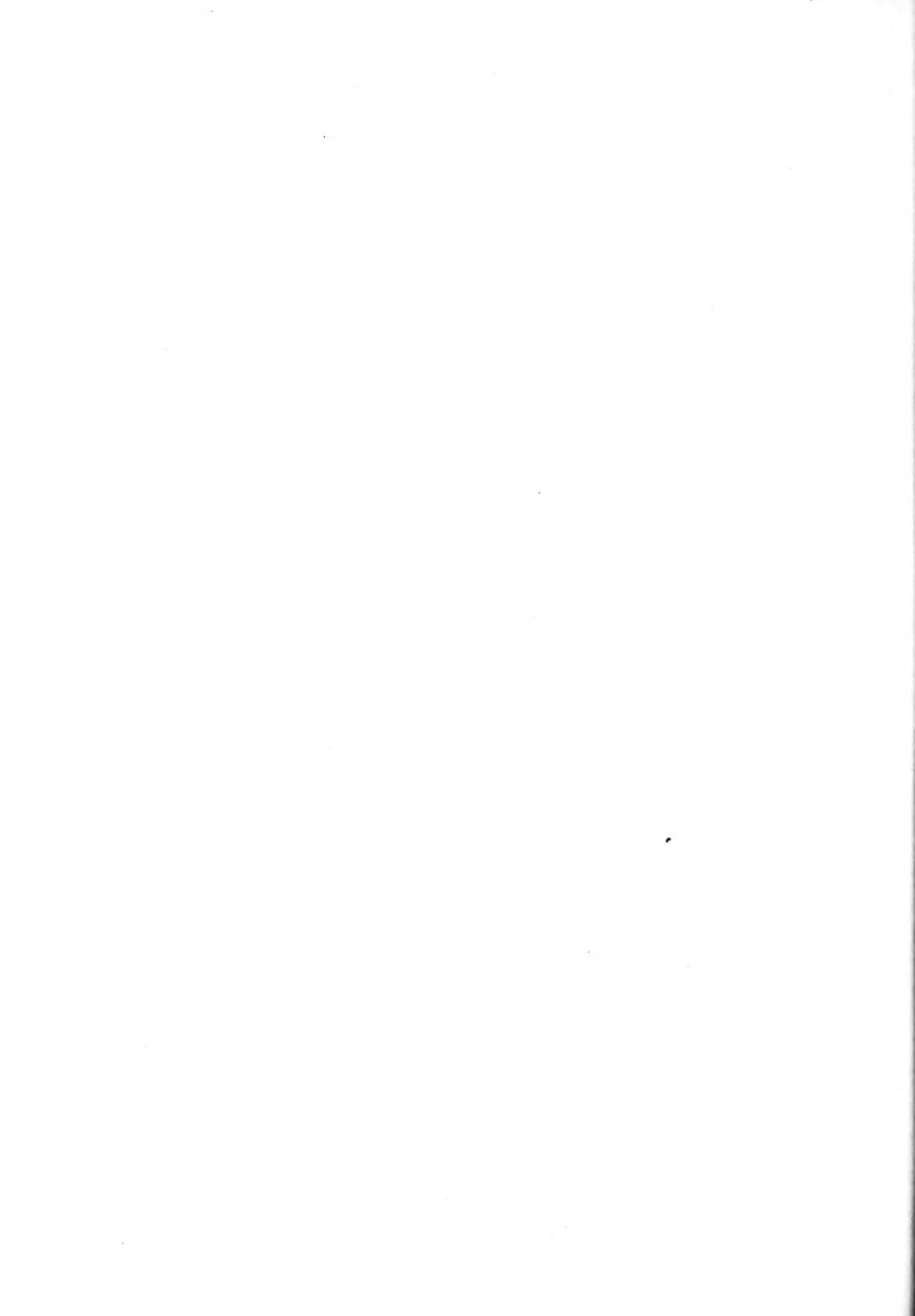
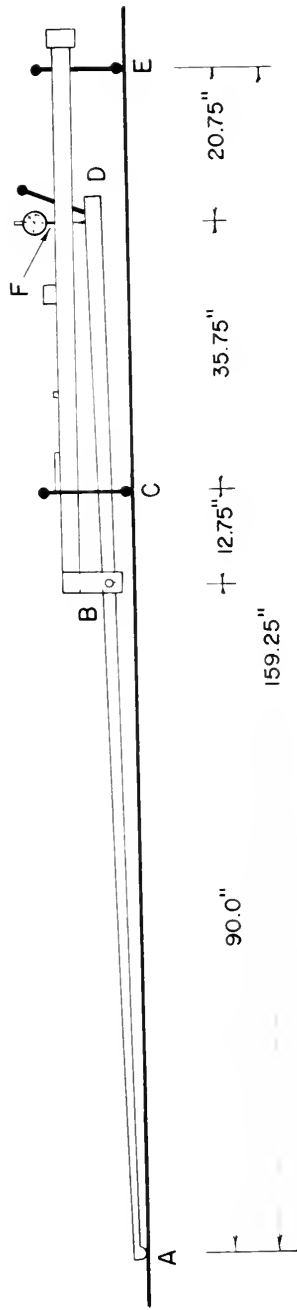


FIGURE 6





BENKELMAN BEAM

FIGURE 7

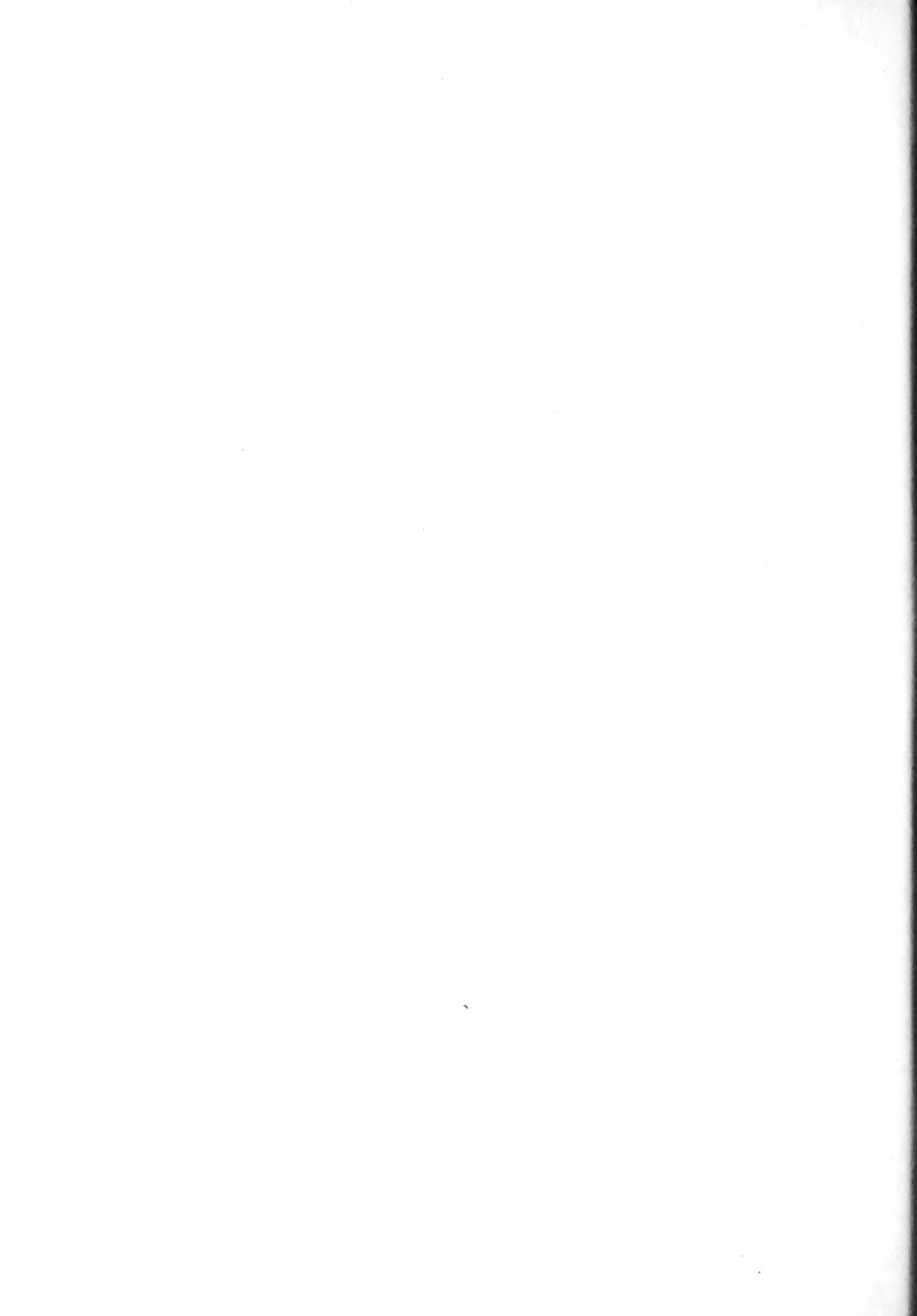


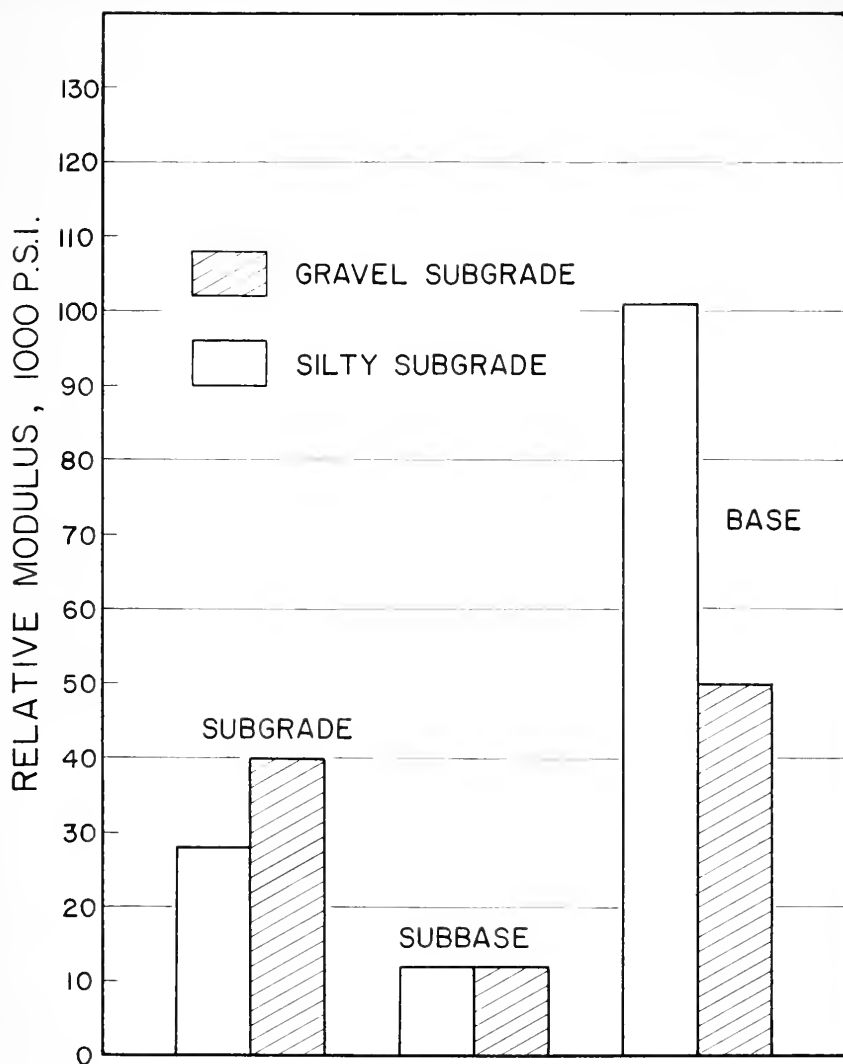
Figure 9 shows typical relative modulus values which are calculated for two locations. It was found that crack frequency could not be correlated with subgrade modulus values, but a relatively good correlation was established between crack frequency and surface texture. In Figure 8 it is seen that the two correlated relatively high modulus values whereas the model is in the middle in general. This is a result of the soil, subgrade.

CONCLUSIONS

The results presented in this report indicate that the structural performance of the pavement is highly dependent on the existing pavement condition under various loading conditions. It has been the purpose of this paper to present a preliminary study which shows the relationship between the

existing pavement condition and the structural performance of the pavement. It is possible to infer structural performance from the existing pavement condition. The relationship will be influenced by type of loading, material, construction, other factors, and the type of construction. The relationship between the existing pavement condition and the structural performance of the pavement is highly dependent on the type of loading, material, construction, other factors, and the type of construction. This was brought out in the study on the U. S. Highway Board of Engineers and Architects. It was found that the relationship between the existing pavement condition and the structural performance of the pavement is highly dependent on the type of loading, material, construction, other factors, and the type of construction. It was not possible to formulate definite conclusions as to the relationship between the existing pavement condition and the structural performance of the pavement. It is indicated that such a relationship should exist.





RELATIVE MODULUS OF PAVEMENT LAYERS
11250 POUND DUAL WHEEL LOAD

FIGURE 9





